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F.K. Choy and Y.K. Tu The University of Akron Akron, Ohio

and

J.J. Zakrajsek and D.P. Townsend Lewis Research Center Cleveland. Ohio



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DYNAMICS OF MULTISTAGE GEAR TRANSMISSION WITH EFFECTS

OF GEARBOX VIBRATIONS

F.K. Choy and Y.K. Tu
Department of Mechanical Engineering
The University of Akron
Akron, Ohio 44325

J.J. Zakrajsek and D.P. Townsend National Aeronautics and Space Administration Lewis Research Center Cleveland, Ohio 44135

SUMMARY

This paper presents a comprehensive approach in analyzing the dynamic behavior of multistage gear transmission systems with the effects of gearbox induced vibrations and mass imbalances of the rotor. The modal method, with undamped frequencies and planar mode shapes, is used to reduce the degrees of freedom of the gear system for time-transient dynamic analysis. Both the lateral and torsional vibration modes of each rotor-bearing-gear stage as well as the interstage vibrational characteristics are coupled together through localized gear mesh tooth interactions. In addition, gearbox vibrations are also coupled to the rotor-bearing-gear system dynamics through bearing support forces between the rotor and the gearbox. Transient and steady state dynamics of lateral and torsional vibrations of the geared system are examined in both time and frequency domains to develop interpretations of the overall modal dynamic characteristics under various operating conditions. A typical threestage geared system is used as an example. Effects of mass imbalance and gearbox vibrations on the system dynamic behavior are presented in terms of modal excitation functions for both lateral and torsional vibrations. Operational characteristics and conclusions are drawn from the results presented.

INTRODUCTION

In the continuous search for the improvements in operational life, efficiency, maintainability, and reliability in gear transmission systems, one of the major objectives in design improvement is the reduction of noise and vibration in the transmission system. Two main streams of work have been carried out in the areas of noise and vibration reduction; namely (1) the localized gear-tooth stress/thermal effects during gear interactions [Cornell 1981, Lin 1988, Boyd 1987, Savage 1986], and (2) the overall global dynamic behavior [August 1986, Choy 1989, David 1987, 1988, Mitchell 1985] of the transmission systems.

The work presented in this paper is the development and application of a comprehensive approach in simulating the overall dynamics of a multistage rotor-bearing-gear system. The modal method is applied to reduce the degrees of freedom of the global system of equations. Various operational characteristics are simulated in the analysis, such as

(1) Multistage rotor-gear configuration

(2) The coupling of gearbox vibrations

(3) The effects of rotor mass-imbalance and shaft bow

(4) The effects of inertia-gyroscopic moments

(5) The effects of nonlinear gear mesh stiffnesses

(6) Variable shaft geometry and bearing support characteristics

The modal equations of motion are solved to evaluate system acceleration at each time step. A self-adaptive variable time-stepping integration technique [Choy 1987, 1988, 1989] is used to calculate the transient dynamics of the system. A typical three-stage rotor-bearing-gear system is used as an example in this analysis. Results are presented in both time and frequency domains to develop a vibration signature analysis of the system.

NOMENCLATURE

$A_i(t)$	modal function of the i th mode in x-direction				
A _{ti} (t)	modal function of the $i^{\mbox{th}}$ mode in $\Theta-\mbox{direction}$				
$B_{i}(t)$	modal function of the i th mode in y-direction				
$[C_T]$	torsional damping matrix				
$[C_{xx}]$, $[C_{xy}]$	bearing direct and cross-coupling damping matrices				
$[C_{yx}],[C_{yy}]$					
F _{Gt} (t)	gear mesh torque				
$F_{Gx}(t), F_{Gy}(t)$	gear mesh force in x- and y-directions				
$F_{t}(t)$	external excitation moment				
$F_{x}(t), F_{y}(t)$	external excitation forces				
$[G_x]$, $[G_y]$	gyroscopic-inertia matrix				
[1]	identity matrix				
[]]	rotational mass moment of inertia matrix				
Ks	shaft stiffness matrix				
$[K_T]$	torsional stiffness matrix				
K _{tki}	gear mesh stiffness between $i^{\mbox{th}}$ and $k^{\mbox{th}}$ rotor				
$[K_{XX}],[K_{XY}]$	bearing direct and cross-coupling damping matrix				
$[K_{yx}],[K_{yy}]$					
[M]	mass-inertia matrix				

R_{Ci} radius of gear in the ith rotor

Tr gear generated torque

 X_{Ci}, Y_{Ci} gear displacements in x- and y-directions of the ith rotor

 X_F,Y_F gear forces in x- and y-directions

angle of tooth mesh between kth and ith rotor

 $[\Lambda^2]$, $[\Lambda^2_t]$ lateral and torsional eigenvalue diagonal matrices

 $[\Phi]_k, [\Phi_t]_k$ lateral and torsional orthonormal eigenvalue diagonal matrices of the k^{th} rotor

DEVELOPMENT OF EQUATIONS OF MOTION

The equations of motion for a single stage multimass rotor-bearing-gear system with the effects of gearbox motion induced vibrations at the bearing supports, rotor inertia and gyroscopic effects, and excitations from rotor mass imbalance and residual runouts can be written in matrix form [Choy 1987, 1989] for the X-Y plane as

$$[M] \{\ddot{X}\} + [G_{X}] \{\dot{X}\} + [C_{XX}] \{\dot{X} - \dot{X}_{b}\} + [C_{XY}] \{\dot{Y} - \dot{Y}_{b}\} + [G_{Y}] \{Y\} + [K_{XX} + K_{S}] \{X\}$$

$$- [K_{XX}] \{X_{b}\} + [K_{XY}] \{Y - Y_{b}\} = \{F_{X}(t)\} + \{F_{GX}(t)\}$$

$$(1)$$

and in the Y-Z plane as

$$[M] \{\ddot{Y}\} - [G_{x}] \{\dot{Y}\} + [C_{yx}] \{\dot{X} - \dot{X}_{b}\} + [C_{yy}] \{\dot{Y} - \dot{Y}_{b}\} - [G_{y}] \{Y\} + [K_{yy} + K_{s}] \{Y\}$$

$$- [K_{yy} \{Y_{b}\} + [K_{yx}] \{Y - Y_{b}\} = \{F_{y}(t)\} + \{F_{Gy}(t)\}$$
 (2)

Here F_X and F_y are force excitations from the effects of mass imbalance, shaft residual bow and bearing support base motion in both X- and Y-directions. The X and Y gear mesh forces, F_{G_X} and F_{G_Y} , are induced from the gear teeth interaction with other coupled gear stages. The bearing forces are evaluated through the relative motion between the rotor $\{X\}$, $\{Y\}$ and the gearbox $\{X_b\}$, $\{Y_b\}$ at the bearing locations [Choy 1987]. The mass-inertia and gyroscopic effects are incorporated in the mass matrix [M] and the gyroscopic matrices $[G_X]$ and $[G_Y]$. The coupled torsional equations of motion for the single rotor- for bearing-gear system can be written as follows:

$$[J]\{\Theta\} + [C_T]\{\Theta\} + [K_T]\{\Theta\} = \{F_T(t)\} + \{F_{C_T}(t)\}$$
(3)

In equation (3), $\{F_T(t)\}$ represents the externally applied torque and $\{F_{Gt}(t)\}$ represents the gear mesh induced moment. Note that equations (1) to (3) repeat for each single gear/rotor stage. The gear mesh forces couple the force equations of each stage to each other as well as the torsional equations to the ty Codes lateral equations [Choy 1989, Cornell 1981, David 1987, 1988]. The coupling



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relationships between the torsional and the lateral vibrations and the dynamics of each individual gear/rotor stage are derived in the next section.

COUPLING IN GEAR MESHES

The torsional and lateral vibrations of a single, individual rotor and the dynamic relationships between each gear stage are coupled through the nonlinear interactions in the gear mesh. Gear mesh forces and moments are evaluated as functions of relative motion and rotation between two meshing gears and the corresponding gear mesh stiffnesses. These gear mesh stiffnesses vary in a repeating nonlinear pattern [August 1986, Cornell 1981, Savage 1986] with each tooth pass engagement period and can be represented by a high order polynomial [Cornell 1981, Boyd 1987]. The periodic nature of such nonlinear mesh stiffnesses can also act as a source of steady state excitation to the gear system. With the coordinate system as shown in figure 1, the following gear mesh coupling equations can be established by equating force and moment [Choy 1989]. For the kth stage gear of the system, summing force in the X-direction results in the following:

$$X_{F} = \sum_{i=1, i \neq r}^{n} K_{tki} \left[-R_{ci} \Theta_{ci} + R_{ck} \Theta_{ck} + (X_{ci} - Y_{ck}) \cos \alpha_{ki} + (Y_{ci} - Y_{ck}) \sin \alpha_{ki} \right] \cos \alpha_{ki}$$

$$+ (Y_{ci} - Y_{ck}) \sin \alpha_{ki} \cos \alpha_{ki}$$

$$(4)$$

Summing force in the Y-direction results in

$$Y_{F} = \sum_{i=1, i \neq k}^{n} K_{tki} [-R_{Ci} \Theta_{Ck} - R_{Ck} \Theta_{Ck} + (X_{Ci} - X_{Ck}) \cos \alpha_{ki} + (Y_{Ci} - Y_{Ck}) \sin \alpha_{ki}] \sin \alpha_{ki}$$
(5)

Summing moment in the Z-direction results in

$$T_{F} = \sum_{i=1, i\neq k}^{n} R_{ck} [K_{tki} (-R_{ci} \Theta_{ci} - R_{ck} \Theta_{ck})]$$
 (6)

where n is the number of stages in the system.

MODAL ANALYSIS

To reduce the computational effort, the number of degrees of freedom of the system of equations is reduced through modal transformation. Orthonormal modes for each individual rotor-bearing stage are obtained by solving the uncoupled system homogeneous characteristic equations. With the modal expansion approach [Choy 1987, 1988, 1989], the motion of the system can be expressed as

$$\{X\} = \sum_{i=1}^{m} A_{i} \{\phi_{i}\}$$
 (7)

$$\{Y\} = \sum_{i=1}^{m} B_{i} \{\phi_{i}\}$$
 (8)

$$\{\Theta\} = \sum_{i=1}^{m} At_{i} \{\phi_{ti}\}$$

$$(9)$$

where m is the number of modes used. The orthogonality conditions of the modes can be expressed as

$$[\Phi]^{\mathsf{T}}[\mathsf{K}][\Phi] = [\Lambda^2] \tag{10}$$

$$\left[\Phi_{t}\right]^{T}\left[K_{t}\right]\left[\Phi_{t}\right] = \left[\Lambda_{t}^{2}\right] \tag{11}$$

$$[\Phi]^{T}[M][\Phi] = [\Phi_{+}]^{T}[J][\Phi_{+}] = [I]$$
 (12)

With the modal expansion and the orthogonality conditions, the modal equations of motion [Choy 1989] can be written as follows:

X-7 equation

$$\{\ddot{A}\} + \{\Phi\}^{T} \{G_{x}\} \{\dot{A}\} + \{\Phi\}^{T} \{C_{xx}\} \{\dot{A}\} + \{\Phi\}^{T} \{C_{xy}\} \{\dot{A}\} + \{\Phi\}^{T} \{G_{y}\} \{\dot{A}\} + \{\Phi\}^{T} \{G_{xy}\} \{\dot{A}\} + \{\Phi\}^{T}$$

Y-Z equation

$$\{\ddot{B}\} - [\Phi]^{T} [G_{x}] [\Phi] \{\dot{B}\} + [\Phi]^{T} [C_{yx}] [\Phi] \{\dot{A}\} + [\Phi]^{T} [C_{yy}] [\Phi] \{\dot{B}\} - [\Phi]^{T} [G_{y}] [\Phi] \{A\}$$

$$+ [\Lambda^{2}] \{B\} + [\Phi]^{T} [K_{yx}] [\Phi] \{A\} = [\Phi]^{T} \{F_{y}(t) + F_{Gy}(t)\}$$

$$(14)$$

Θ-equation

$$\{\ddot{A}_{t}\} + [\Phi_{t}]^{T}[C_{T}][\Phi_{t}]\{\dot{A}_{t}\} + [\Lambda_{t}^{2}]\{A_{t}\} = [\Phi_{t}]^{T}\{F_{t}(t) + F_{Ct}(t)\}$$
(15)

The gear mesh forces and moment can also be expressed in the modal form, for the \mathbf{k}^{th} stage, as follows:

$$[\Phi]_{k}^{T} \{Y_{F}\} = \sum_{j=1}^{m} \phi_{kj} \left\{ \sum_{i=1,1-k}^{n} K_{tki} [-R_{ci}\theta_{ci} - R_{ck}\theta_{ck} + (x_{ci} - x_{ck})\cos\alpha_{ki} + (y_{ci} - y_{ck})\sin\alpha_{ki} \right\}$$

$$+ (y_{ci} - y_{ck})\sin\alpha_{ki}$$

$$(17)$$

$$[\Phi]_{k}^{T} \{T_{F}\} = \sum_{j=1}^{m} \phi_{kjl} \left\{ \sum_{l=1, l-k}^{n} R_{ck} [K_{tki} (-R_{ci} \Theta_{ci} - R_{ck} \Theta_{ck})] \right\}$$
 (18)

where K is the stage number, j is the mode number, and l is the station location of the gear mesh.

SOLUTION PROCEDURE

Rearrange the modal equations of motion developed in equations (13) to (15) into the following:

X-equation

$$\{\ddot{A}\} = -[\Phi]^{T}[G_{x}][\Phi]\{\dot{A}\} - [\Phi]^{T}[C_{xx}][\Phi]\{\dot{A}\} - [\Phi]^{T}[C_{xy}][\Phi]\{\dot{B}\} - [\Phi]^{T}[G_{y}][\Phi]\{\dot{B}\}$$
$$- [\Lambda^{2}]\{A\} - [\Phi]^{T}[K_{xy}][\Phi]\{B\} + [\Phi]^{T}\{F_{x}(t) + F_{Gx}(t)\}$$
(19)

Y-equation

$$\{\ddot{B}\} = [\Phi]^{T}[G_{x}][\Phi]\{\dot{B}\} - [\Phi]^{T}[C_{yx}][\Phi]\{\dot{A}\} - [\Phi]^{T}[C_{yy}][\Phi]\{\dot{B}\} + [\Phi]^{T}[G_{y}][\Phi]\{B\}$$

$$- [\Lambda^{2}]\{B\} - [\Phi]^{T}[K_{yx}][\Phi]\{A\} + [\Phi]^{T}\{F_{y}(t) + F_{Gy}(t)\}$$

$$(20)$$

0-equation

$${\ddot{A}_{t}} = -[\Phi_{T}]^{T}[C_{T}][\Phi_{t}]{\dot{A}_{t}} - [\Lambda_{t}^{2}]{\dot{A}_{t}}[\Phi_{t}]^{T} + {F_{t}(t) + F_{Gt}(t)}$$
(21)

A variable time stepping Newmark-Beta integration scheme evaluates the modal velocity and displacement at each time interval. In turn, equations (7) to (9) transform the modal displacements into absolute relative displacements in fixed coordinates. The gear mesh forces can be evaluated by the relative motion between the gear teeth using the nonlinear stiffnesses developed for the gear mesh interaction. The effects of gearbox vibration can be calculated as nonlinear bearing forces through the relative vibration between the gearbox and

the shaft at the bearing locations. Since the gearbox and the shaft both are vibrating independently, a separate transient integration scheme is required for each system at every time step before the coupling of bearing forces.

DISCUSSION OF RESULTS

To demonstrate the application of the discussed analytical method, a typical three-stage gear transmission given in figure 2 is used as an example. All three gear stages have an identical 36-tooth gear and a mesh contact ratio of 1.6. Stage I of the system is the driver with a rotational speed of 3000 rpm and an input torque of 2.25 kN-m. Both stages I and II are supported by three bearings while stage III only has two bearing supports. The first two bearings in stages I to III and the third bearings in stages I and II are identical. The rotor in stages I and II is 2.4 in. (6.1 cm) in diameter and has a length of 40 in. (101 cm) and 30 in. (76 cm), respectively. The rotor in stage III is smaller with a diameter of 1.4 in. (3.5 cm) and a length of 20 in. (51 cm). For demonstration purposes, the first three basic modes of the system are used in the modal analysis. Table I provides the information on the modal frequencies of the system in both lateral and torsional directions. Figures 3 and 4 give the orthonormal mode shapes of the first two basic torsional and lateral modes for all three rotor stages. Note that the general form of mode shapes in stage I is more like a mirror image compacted to those of stages II and III which are generally identical. This is due to the fact that a nominal support stiffness is assumed at the gear locations, which produce a substantial difference on the vibratory modes of each rotor stage.

In order to investigate the effects of gearbox vibrations and rotor mass imbalance, results from four major cases of external excitations are examined in this study, namely

Case 1. - No gearbox vibration and small mass imbalance

Case 2. - Gearbox vibration and small mass imbalance

Case 3. - No gearbox vibration and large mass imbalance

Case 4. - Gearbox vibration and large mass imbalance

The gearbox vibrational effects are assumed to be a steady state vibration motion of 1200 Hz at the bearing supports. Vibrational orbits of all three rotor stages at the gear location for all four cases, respectively, are given in figures 5 to 7. Note that the vibratory characteristics of stage I is more influenced by mass imbalance while those of stages II and III are affected by motion of the gearbox through the bearing supports. As we can see from figure 5(b), the effects of bearing support motion to stage I gear vibrational orbits are quite small. This is due to the fact that the rotor of stage I is substantially more flexible than the other two rotors and less influence from the bearing can be effectively converted to the system. In addition, although similar mass imbalances are applied to each rotor stage, vibratory orbits in stages II and III are smaller in amplitude because of their larger rotor stiffnesses.

Figures 8 to 10 depict the first modal component of rotor stages I to III. respectively. Figure 8 shows the effects of the four external excitations on the first modal vibratory component of stage I in both time and frequency domains. Note that figures 8(a) and (b) show that, for small imbalance with no gearbox motion, only very small vibratory motion will result except for the

dc component at zero frequency. Figures 8(c) and (d) represent the first mode rotor vibrations resulting from gearbox motion. Note that the major component occurs at 1200 Hz (input vibratory frequency at the bearing supports) with a minor component at 115 Hz (first natural frequency of stage I). Figures 8(e) and (f) show the effect of mass imbalance, which results in a large component at the rotor speed of 50 Hz and a smaller component at the first mode of 115 Hz. Figures 8(g) and (h) produce the combined effect of gearbox vibration and imbalance on rotor first mode vibrations. By examining the relative amplitudes of the major components, rotor speed, and gearbox vibration frequency, with their corresponding input excitation magnitude, the sensitivity of the rotor to imbalance and gearbox vibration can be determined. Similar conclusions can be arrived in figures 9 and 10 for stages II and III, except that the effects of mass imbalance on first mode vibration is significantly reduced. As we can see in figures 9(g) and (h) and 10(g) and (h), when both excitations are present. the gearbox motion has a much more dominating affect in rotor vibration for stages II and III as compared to stage I. Figures 11 to 13 show the vibration of the second mode component for the three rotor stages, respectively. Note in figure 11, for stage I the second mode vibrational characteristics are very similar to those of the first mode. However, magnitudes of the second mode are approximately 20 percent of those of the first mode. This is because the first mode in the first stage is more easily excited by the imbalances and gear forces acting at the gear location. Further examinations of figures 12 and 13 show that the second mode is more excited than the first mode in the second and third rotor stages. A more detailed study of figures 3 and 4 reveals that the second mode in stages II and III is very similar to the shape of the first mode in stage I, which is the first fundamental bending mode of the overhung rotor system. In addition, from figures 8 to 13, it was found that none of the torsional vibratory frequencies and gear meshing frequencies are excited in the lateral rotor vibration of the system.

Figure 14 depicts the gear mesh forces with effects of both imbalance and gearbox motion excitations. Note that the major component of these forces is the dc component at zero frequency which is due to the constant applied torque. The other sizable force component is at the tooth meshing frequency of 1800 Hz. The higher ac component which results in higher meshing frequency component between gears I and III, is because of the lower rotational stiffness in the stage III rotor. This can also be observed by the higher dc (zero frequency component) in stage III compared to stage II, as shown in figures 15 and 16. Only a very small force component can be observed at the gear mesh frequency (1800 Hz) and first mode frequencies of stage I (355 Hz), stage II (550 Hz). and stage III (280 Hz). Again figures 15 and 16 outline the modal rotational vibration characteristics of all rotor stages with both excitations. Note in figure 15 that other than the zero frequency component, the other sizable vibration is at its own rotational modal frequency (i.e., 355 Hz at stage 1, 550 Hz at stage II, and 280 Hz at stage III). Figure 16 depicts the second mode rotational vibration characteristics. Note that similar conclusions can be reached for the second modal frequencies of 1090, 1610, and 820 Hz, respectively, for stages I to III.

SUMMARY OF RESULTS

This paper presents a vibration analysis with the effects of gearbox motion and mass imbalance for multistage gear transmission. The analysis

combines gear mesh dynamics and structural modal analysis to study the transmission vibrations. The major content of this work can be summarized as follows:

- 1. A comprehensive approach is developed to combine the nonlinear gear mesh dynamics with structural, lateral, and torsional vibration of the system to determine the global system response.
- 2. The modal method transforms the equations of motion into modal coordinates to reduce the degrees of freedom of the system of equations.
- 3. Gear force observations in both the time and frequency domains provide good insights into the source of dominating response forces.
- 4. The magnitude of the gear mesh force is inversely proportional to the rotor stiffness of the geared system.
- 5. The influence of the gearbox motion to system vibration is more pronounced in a stiffer rotor system.
- 6. Gear tooth mesh frequency and torsional modal frequencies have substantial effects on rotational but not on lateral vibrations of the system.
- 7. Knowledge of modal amplifications under various excitations provide an understanding of the vibrational characteristics of the system. This knowledge is crucial for designing transmissions with improved performance and durability.

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TABLE I. - SYSTEM NATURAL FREQUENCIES

Mode	Stage I	Stage II	Stage III				
Torsional natural frequencies, Hz							
1 2	355 1090	550 1610	280 820				
Lateral natural frequencies, Hz							
1 2 2	115 145 190	160 189 264	110 200 160				

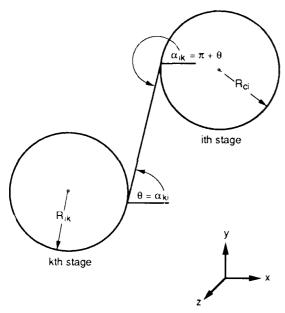


Figure 1.—Coordinate system for gear mesh force.

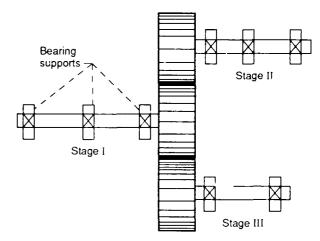


Figure 2.—Three-stage rotor-bearing gear system.

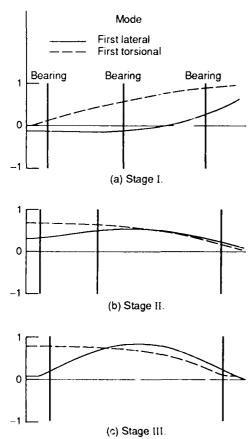


Figure 3.—First vibration mode of three-stage system.

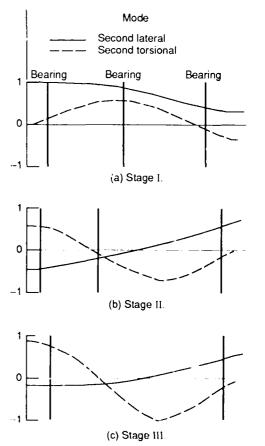


Figure 4.—Second vibration mode of threestage system.

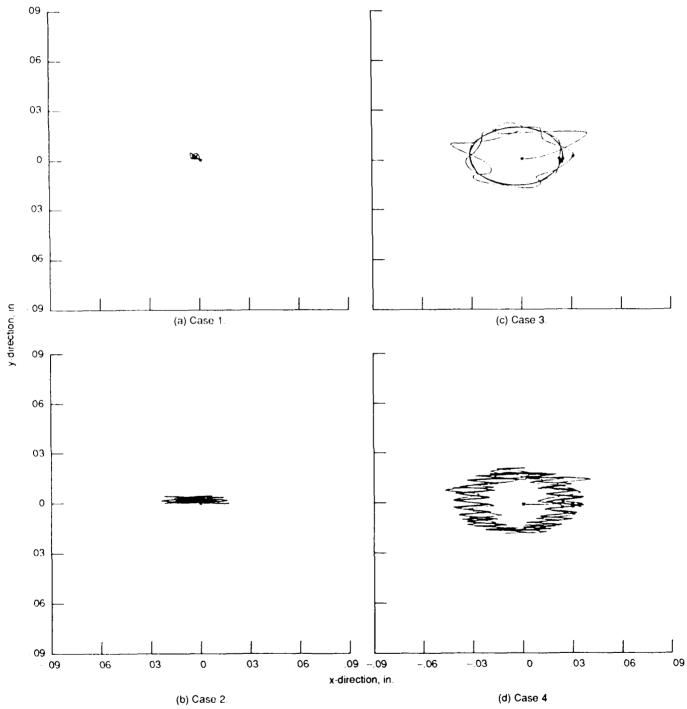


Figure 5.—Stage I rotor vibrational orbit.

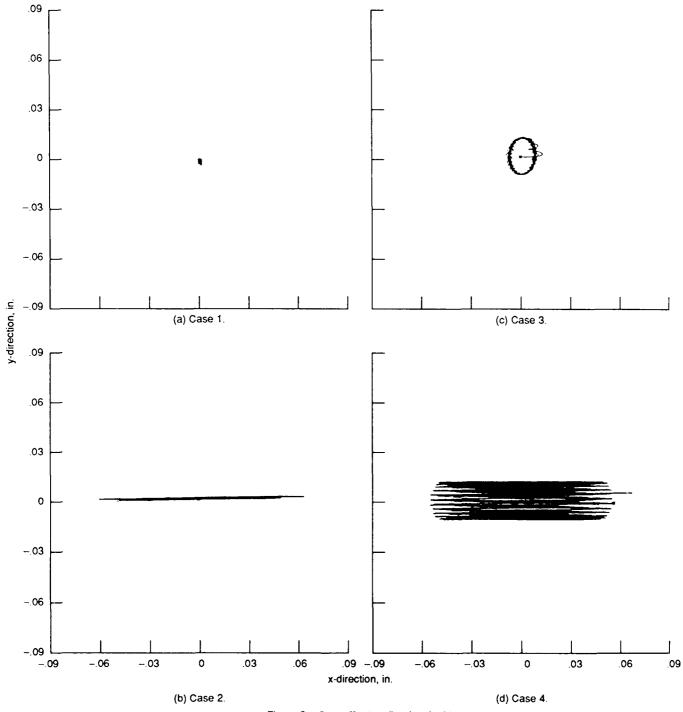


Figure 6.—Stage II rotor vibrational orbit.

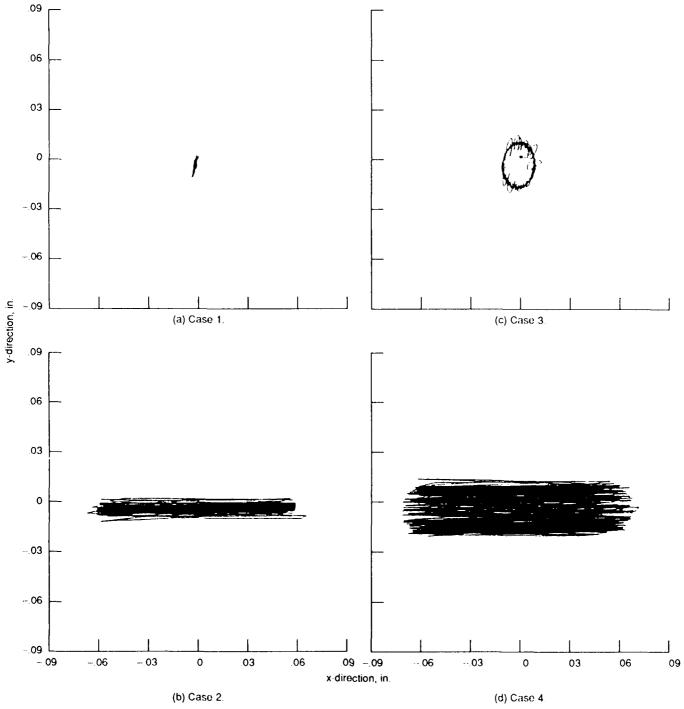


Figure 7.-- Stage ItI rotor vibrational orbit.

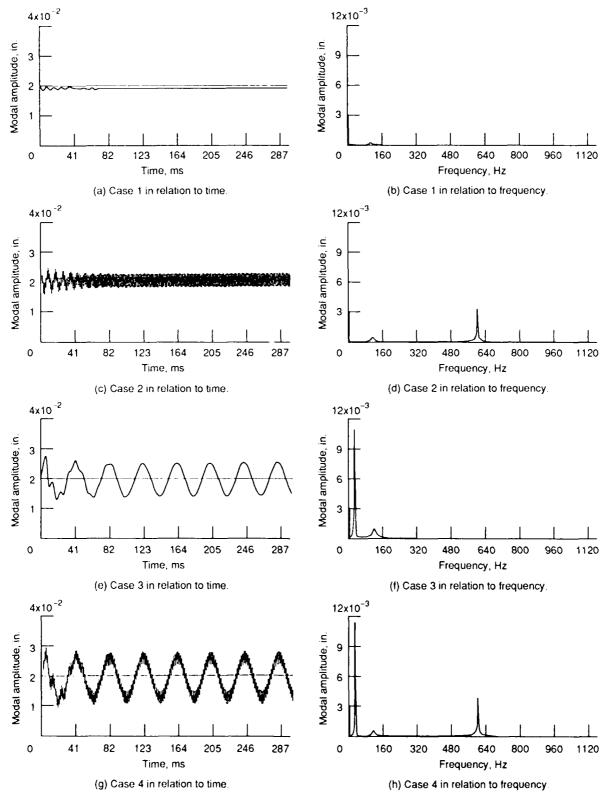


Figure 8.—First lateral modal excitation on stage I.

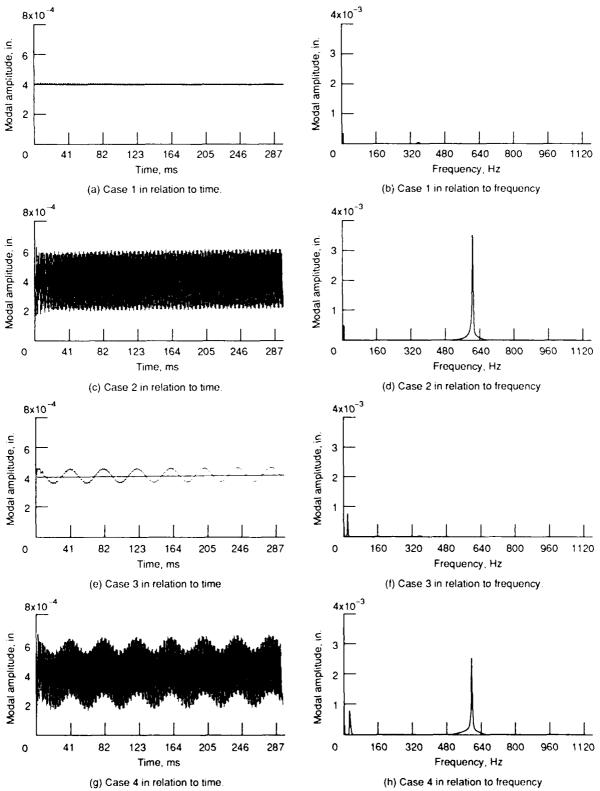


Figure 9.—First lateral modal excitation on stage II.

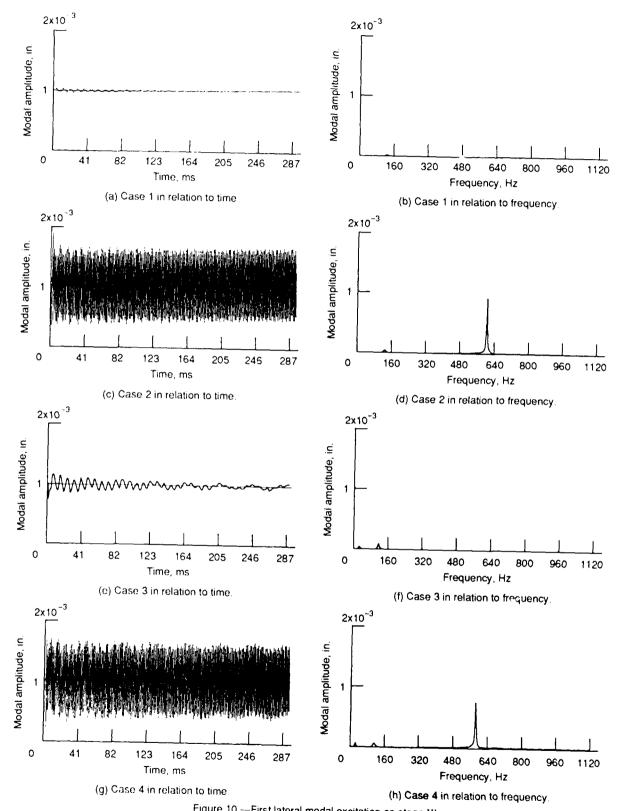


Figure 10 —First lateral modal excitation on stage III.

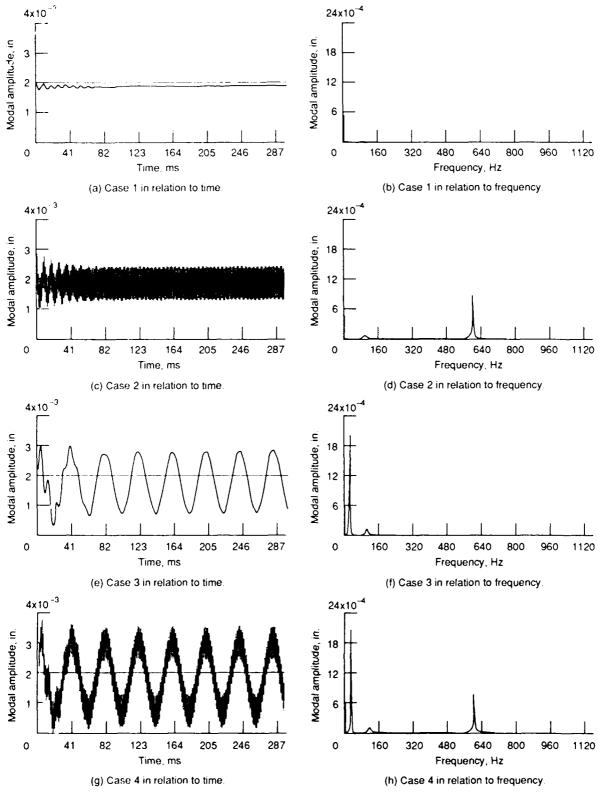


Figure 11.—Second lateral modal excitation on stage I

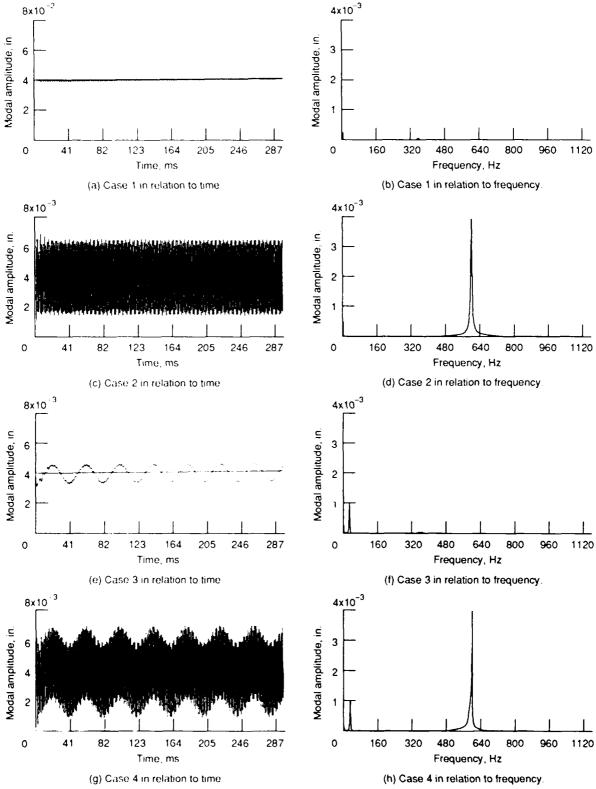


Figure 12 -- Second lateral modal excitation on stage II.

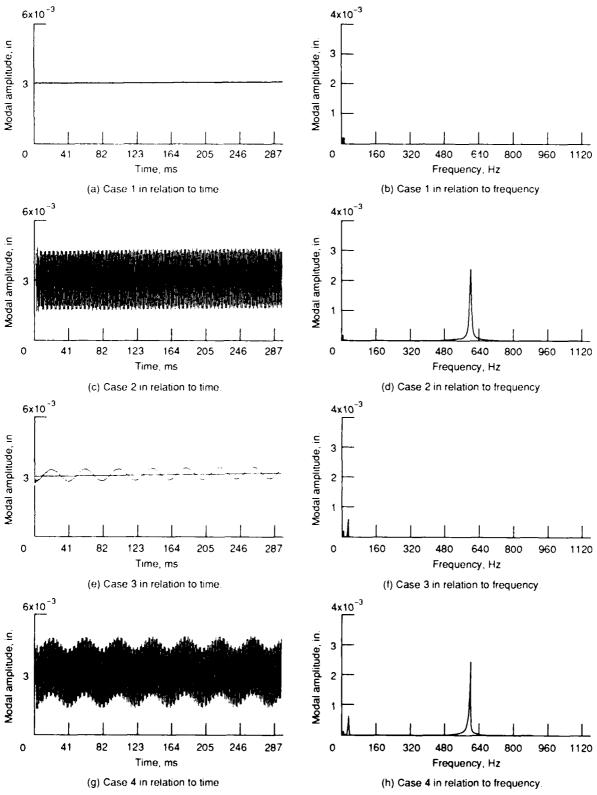


Figure 13 -- Second lateral modal excitation on stage III.

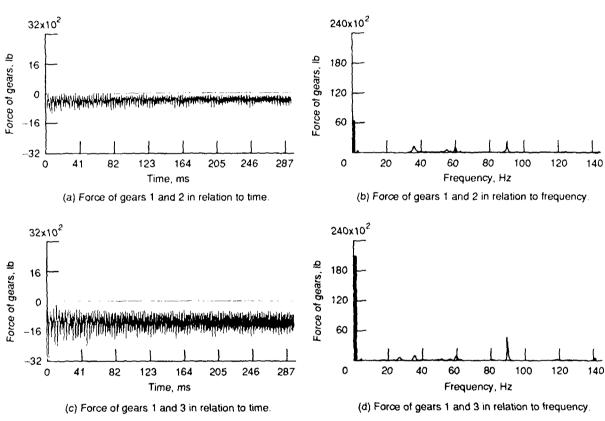


Figure 14.—Gear force in time and frequency domains.

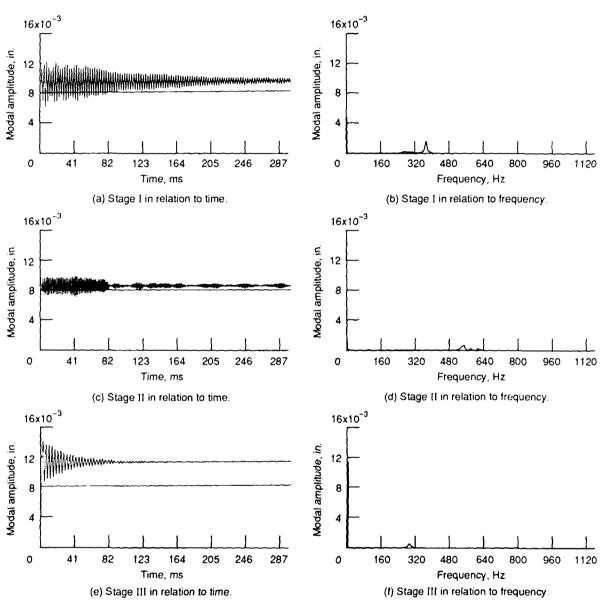


Figure 15.—First torsional modal excitation on stage I.

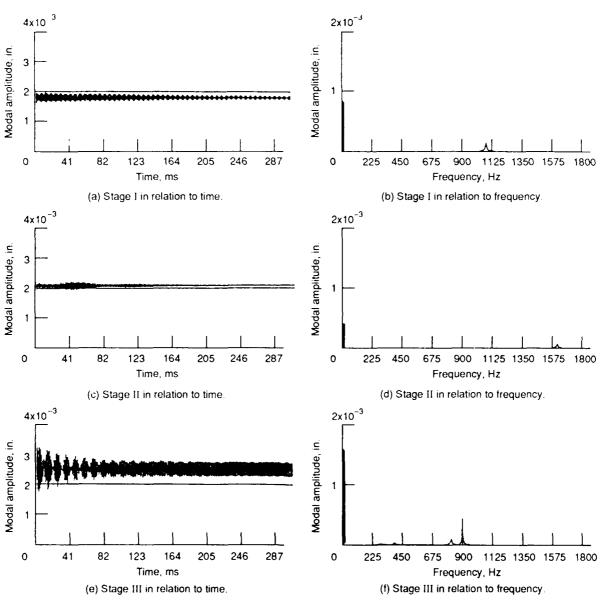


Figure 16.—Second torsional modal excitation on stage I.

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16. Abstract			· · · · · · · · · · · · · · · · · · ·				
This paper presents a comprehensive a systems with the effects of gearbox in undamped frequencies and planar mod time-transient dynamic analysis. Both well as the interstage vibrational charactions. In addition, gearbox vibration bearing support forces between the rot torsional vibrations of the geared system pretations of the overall modal dynam geared system is used as an example, behavior are presented in terms of mocharacteristics and conclusions are dra	duced vibrations and le shapes, is used to the lateral and torsion acteristics are coupled as are also coupled to tor and the gearbox, are examined in the ic characteristics und Effects of mass imbated all excitation functions	mass imbalances of reduce the degrees and vibration mode d together through the rotor-bearing- Transient and stead both time and frequiler various operating alance and gearbox ons for both lateral	of the rotor. The mo- of freedom of the g s of each rotor-bear localized gear mesh gear system dynamics by state dynamics of ency domains to de- g conditions. A typic vibrations on the sy	dal method, with gear system for ing-gear stage as tooth interest through Tlateral and velop interecal three-stage estem dynamic			
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